

2025

Time :As in Programme

Full Marks : 25

The figures in the right-hand margin indicate marks.

*Answer **all** the questions*

PART-I

1. Answer all questions

1x5

ସମସ୍ତ ପ୍ରଶ୍ନର ଉତ୍ତର ଦିଅ ।

a. Education for character building.

ଚରିତ୍ର ଗଠନରେ ଶିକ୍ଷାର ଭୂମିକା ।

b. Ragging as a cause of mental trauma.

ରାଗିଂ ମାନସିକ ଆଘାତର ଏକ କାରଣ ।

c. Define plagiarism.

ପ୍ଲାଗିଆରିଜମର ସଂଜ୍ଞା ଲେଖ ।

d. What is Positive friendship ?

ସକାରାତ୍ମକ ବନ୍ଧୁତ୍ବ କ'ଣ ?

e. Define co-curricular activities.

ସହଗ-ପାଠ୍ୟକ୍ରମର ସଂଜ୍ଞା ଲେଖ ।

PART-II

2. Answer any five of the following questions.

2x5

ନିମ୍ନଲିଖିତ ପ୍ରଶ୍ନଗୁଡ଼ିକ ମଧ୍ୟରୁ ଯେକୌଣସି ପାଞ୍ଚଟି ପ୍ରଶ୍ନର ଉତ୍ତର ଲେଖ ।

a. Explain, "Failed in examination but passed life".

“ପରୀକ୍ଷାରେ ଅକୃତକାର୍ଯ୍ୟ, ଜୀବନରେ କୃତକାର୍ଯ୍ୟ” – ବୁଝାଅ ।

b. What is cognitive-behavioural counselling ?

ଜ୍ଞାନାତ୍ମକ-ବ୍ୟାବହାରିକ ପରାମର୍ଶ କ'ଣ ?

(Turn Over)

- c. Major conflicts among college students.
ମହାବିଦ୍ୟାଳୟ ଛାତ୍ରମାନଙ୍କର ପ୍ରମୁଖ ଦ୍ଵନ୍ଦ୍ଵ ।
- d. Hostel life as independent but responsible.
ଛାତ୍ରାବାସ ଜୀବନ ସ୍ଵାଧୀନ କିନ୍ତୁ ଦାୟିତ୍ଵପୂର୍ଣ୍ଣ ।
- e. Teacher-student relationship.
ଗୁରୁ-ଶିଷ୍ୟଙ୍କ ସମ୍ପର୍କ ।
- f. Define leadership.
ନେତୃତ୍ଵର ସଂଜ୍ଞା ଲେଖ ।
- g. Benefits of co-curricular activities for students.
ଛାତ୍ରମାନଙ୍କ ପାଇଁ ସହଗ-ପାଠ୍ୟକ୍ରମର ଉପାଦେୟତା ।

PART-III

3. Answer any two of the following questions.

5x2

ନିମ୍ନଲିଖିତ ପ୍ରଶ୍ନଗୁଡ଼ିକ ମଧ୍ୟରୁ ଯେକୌଣସି ଦୁଇଟି ପ୍ରଶ୍ନର ଉତ୍ତର ଦିଅ ।

- a. "Knowledge is power" - Explain with examples.
"ଜ୍ଞାନ ହିଁ ଶକ୍ତି" - ଉଦାହରଣ ସହ ଆଲୋଚନା କର ।
- b. "Violence vs. Peaceful protest" - Give your debate.
"ହିଂସା ବନାମ ଶାନ୍ତିପୂର୍ଣ୍ଣ ଓ ପ୍ରତିବାଦ" ବିତର୍କ ଲେଖ ।
- c. "Cheating in examinations is cheating yourself". Explain.
"ପରୀକ୍ଷାରେ ଠକିବା ନିଜକୁ ଠକିବା ସହ ସମାନ" - ଆଲୋଚନା କର ।
- d. "Positive interpersonal relation is the strength of life". Explain.
"ସକାରାତ୍ମକ ପାରସ୍ପରିକ ସମ୍ପର୍କ ଜୀବନର ଶକ୍ତି" - ଆଲୋଚନା କର ।
- e. Describe scope of leadership for college students.
ମହାବିଦ୍ୟାଳୟ ଛାତ୍ରମାନଙ୍କର ନେତୃତ୍ଵ ନେବାର ସୁଯୋଗଗୁଡ଼ିକୁ ବର୍ଣ୍ଣନା କର ।



2025

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*Answer **all** questions.*

PART-I

1. Answer all Questions.

1x8

- a. The heat of neutralisation of 1 mole of strong acid in dilute solution with one mole of strong base is ____.
- b. What happens to the entropy of spontaneous process.
- c. pH of pure water ____ with rise of temperature.
- d. The solubility of CaF_2 is $3.2 \times 10^{-11} \text{M}^3$, its solubility is ____.
- e. What is the product when benzene reacts with chlorine in the sun light ?
- f. Phenol when heated with Zn produces ____.
- g. What is the electrophile in Friedel Craft alkylation reaction ?
- h. Which types of aldehyde undergo aldol condensation reaction ?

(Turn Over)

PART-II

2. Answer any eight within two to three sentences 1.5x8
- Define an isolated system ?
 - What is Gibb's Helmholtz equation ?
 - Explain why cloths dry quicker when there is breeze.
 - Why pH of solution of potassium acetate is more than 7 ?
 - Define solubility product.
 - What is nitrating mixture ?
 - Give one example each of o- & p- directing and m-directing group.
 - Between benzene and toluene which is more reactive towards electrophilic substitution reaction and why ?
 - How could you distinguish between Butan-2-one and butan-3-one ?
 - Explain why boiling point of dimethyl ether is lower than that of ethyl alcohol.

PART-III

3. Answer any eight of the following (in maximum 75 words.) 2x8
- Calculate the heat of reaction of the following reaction.



Bond energy of C-H, F-F, C-F and H-F bonds are 415.5, 159.5, and 564.8 kJ/mol respectively.

- b. What would happen to a reversible reaction at equilibrium when
- (i) Temperature is raised, given that its ΔH is +ve
 - (ii) Pressure is lowered given that Δn is +ve.
- c. Why zinc sulphide is precipitated by H_2S from solution of zinc acetate but not solution of zinc chloride ?
- d. What happens when HCl gas is passed through a saturated solution of barium chloride ?
- e. Calculate the pH of 10^{-8} M HCl .
- f. Write the mechanism of chlorination of benzene.
- g. How can you prepare acetophenone from benzene ?
- h. What is Fehling solution ? How does it react with aldehyde ?
- i. How can you prepare benzaldehyde by Etard's reaction ?
- j. Give the reaction of phenol with $CHCl_3$ in presence of aq. $NaOH$.

PART-IV

Answer within 500 words each.

6x4

4. State and explain Hess's law of constant heat summation.
Discuss its application.

4+2

OR

Define Le Chatelier's principle and how is it applied in manufacture of ammonia ?

2+4

(3)

(Turn Over)

5. What do you mean by Hydrolysis of salt ? Predict whether the aqueous solution of sodium carbonate will be acidic, neutral or alkaline, Explain why ? 2+4

OR

Write a note on buffer solution. A 0.1 MHCN solution contained 0.2 mole KCN per litre of solution. Calculate the $[H^+]$ of the solution (K_a of HCN = 7.2×10^{-10}) 4+2

6. a. How benzene is prepared from acetylene ? How does it react with 2+2+2
(i) Cl_2 in presence of $AlCl_3$ (ii) Conc. H_2SO_4 .

OR

- b. Write notes on : (i) Sandmeyer's reaction (ii) Huckel's rule 4+2
7. How you can prepare acetaldehyde from ethyl alcohol ? What happens when acetaldehyde reacts with 2+2+2
- a. CH_3MgBr (ii) H_2O/H^+
- b. Phenyl Hydrazine ?

OR

How Primary, Secondary and Tertiary Alcohols can be distinguished by Lucas test ? What happens when excess of ethyl alcohol is heated with conc. H_2SO_4 at $140^\circ C$.



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*Answer **all** questions.*

PART-I

1. Answer all Questions. 1x8
 - a. If 'x' is the true value and 'a' be an approximation to x then relative error is _____.
 - b. Suppose the number 0.025 is approximated by 0.02. Find percentage error.
 - c. In Gauss Jordan method system of equation $AX=b$ reduces to $DX=b$ where D is _____ matrix.
 - d. Why Newton - Raphson method is superior to bisection method for finding the numerical solution of non linear equation ?
 - e. The interpolating polynomial $P(x)$ that interpolate $f(x)$ at $x_0, x_1 \dots x_n$ is at most degree _____.
 - f. Write the relation between forward difference operator and the shift operator.
 - g. The mid point rule formula for $\int_a^b f(x)dx =$ _____.
 - h. Write trapezoidal rule with error term.

(Turn Over)

PART-II

2. Answer any eight questions.

1.5x8

- a. Round off the number 0.000455 correct upto three significant figures.
- b. Find the interval in which the root of equation $x^2=3$ lies.
- c. Write iteration function to find the root of the equation $x^3+x^2-1=0$ using fixed point iteration method.
- d. Write the system of equation in $AX=b$ form to find A, X and b :
- e. Show that divided difference of a constant is zero.
- f. Write Lagrange's Polynomial $li(x)$ at $(n+1)$ distinct points x_0, x_1, \dots, x_n and write its properties.
- g. What is the difference between Gaussian elimination method and Gauss. Jordan elimination method for solving system of linear equations ?
- h. Write Newton cotes Quadrature formula involving $(n+1)$ nodes x_0, x_1, \dots, x_n with $W_i x_0 = x_0 + \alpha h, 0 \leq \alpha \leq h$
- i. Define extrapolation.
- j. Write composite formula for Simpson's $\frac{1}{3}$ Rule $a=x_0 < x_1 < \dots < x_{2n-1} < x_{2n} = b$ and it's error term.

PART-III

3. Answer any eight of the following questions.

2x8

- a. Perform four iteration to find an approximation to $x^2=3$ using bisection method.
- b. Using 5 - digits floating point arithmetic, find the product

of $\frac{1}{3}$ and $\frac{5}{7}$.

18625

c. Derive formula for Newton Raphson method to find approximation to root of $f(x)=0$

d. Find the eigen values of $\begin{bmatrix} 1 & 2 & -2 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix}$.

e. Solve the equation by Gauss Jordan method, $x + y = 0$, $y + z = 1$, $x + z = 3$.

f. Is Pivoting always necessary for solving system of linear algebraic equations ? Justify your answer.

g. Show that $\mu^2 = 1 + \frac{\delta^2}{4}$.

h. Show that $\delta = \nabla (1 - \nabla)^{\frac{1}{2}}$

i. Derive Simpson's $\frac{1}{3}$ rule for $x_0=a$, $x_1 = \frac{a+b}{2}$, $x_2 = b$ and $n=2$.

j. Given the following values of $f(x)=\ln x$. Find the approximate value of $f'(2.0)$ using linear interpolation.

i	0	1	2
x_i	2.0	2.2	2.6
f_i	0.69315	0.78846	0.95551

PART-IV

Answer all questions.

6x4

4. Find the smallest positive root of the equation $x^3 - 5x + 3 = 0$ by Newton Raphson method by taking four iterations.

OR

Find the approximate root correct upto two decimal places of equation $x^2 = 3$ by Secant method.

MAT-223(4)

2.06640 (3)

34.38 (Turn Over)

34.3281

4.2910

(3.25)

2.0664

5. Find the inverse of the co-efficient matrix of the system.

$$\begin{bmatrix} 1 & 1 & 1 \\ 4 & 3 & -1 \\ 3 & 5 & 3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 6 \\ 4 \end{bmatrix} \text{ by}$$

Gauss - Jordan method with partial Pivoting and hence solve the system.

OR

If A is strictly diagonally dominant matrix, then show that the Gauss-Seidel iteration Scheme Converges for any initial Starting vector.

6. From table of Logarithm find interpolating polynomial of $\log x$ and find $\log 1.25$ by Newton Divided Difference.

x	1.0	1.5	2.0	2.5
$\log x$	0	0.17609	0.30103	0.39794

OR

Derive Newton forward difference interpolating polynomial of $f(x)$ at $x_0 = a, x_1, \dots, x_n = b, x_i = x_0 + ih$.

7. Derive Newton - Cotes rules and find its error.

OR

Using six intervals of equal length, obtain the approximate value

of $\int_0^1 \frac{dx}{1+x}$ by Simpson's $\frac{1}{3}$ rule.



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2436*

2025

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*Answer **all** questions.*

PART-I

1. Answer all Questions. 1x12
- a. Write the characteristics of Ring R .
 - b. Is $Z \oplus Z$ is an integral domain ? (Yes/No).
 - c. The polynomial x^2+1 is reducible over ____.
 - d. Is the mapping Z_5 to Z_{30} given by $x \rightarrow 6x$ a ring homomorphism ? (Yes/No)
 - e. Give an example of integral domain which is not UFD.
 - f. The characteristic of an integral domain is a prime only. (True/false)
 - g. $\{2,0,4\}$ is a subring of the ring Z_6 , the integers of modulo 6. (True/false)
 - h. If the leading coefficient of a Polynomial $f(x) \in R[x]$ is the multiplicative identity of $R[x]$ then $f(x)$ is called ____ Polynomial.
 - i. Is the Polynomial $f(x)=2x^2+4$ irreducible over Z ? Yes/no.
 - j. $f(x)=x^2+1$ has zero in Z_3 (True/false)
 - k. Is the ring Z is a Euclidean domain ? (Yes/ no)
 - l. Find the idempotent in Z_{10} .

(Turn Over)

PART-II

2. Answer any eight questions.

2x8

- a. Let $a \in$ a ring R , prove that $0a=a0=0$.
- b. If R has a Unity element 1 , then prove that $(-1)a=-a$.
- c. Define a field.
- d. When an integral domain is said to be a Unique factorization domain?
- e. Define Kernel of a ring homomorphism R .
- f. Show that \mathbb{R} , the set of real numbers is a subring of \mathbb{C} .
- g. Define principal Ideal domain.
- h. Find all maximal ideals of $\mathbb{Z}_8 \oplus \mathbb{Z}_{30}$.
- i. Define associates of an integral domain.
- j. Define Unique Factorization domain.

PART-III

3. Answer any eight of the following questions.

3x8

- a. If $a, b \in R$, Prove that $(-a)(-b)=ab$ where R is a ring.
- b. If ϕ is a homomorphism of a ring R into a ring R with Kernel S , then show that S is an ideal of R .
- c. Find all units, zero divisor, idempotents and nilpotent elements in $\mathbb{Z}_3 \oplus \mathbb{Z}_6$.
- d. Let F be a field. If $f(x) \in F[x]$ and $\deg f(x)=2$ or 3 , then prove that $f(x)$ is reducible over F iff $f(x)$ has a zero in F .
- e. Prove that $\phi: x \rightarrow 5x$ from \mathbb{Z}_4 to \mathbb{Z}_{10} is a ring homomorphism.
- f. Explain why every subgroup of \mathbb{Z}_n under addition is also a subring of \mathbb{Z}_n ?
- g. List all the Polynomials of degree 2 in $\mathbb{Z}_2[x]$ which of these are equal as functions from \mathbb{Z}_2 to \mathbb{Z}_2 .

- ✓ h. Give an example of commutative ring that has a maximal ideal but is not a prime ideal.
- ✓ i. Prove that every Euclidean domain is a principal ideal domain.
- j. Show that $1-i$ is an irreducible in $\mathbb{Z}[i]$.

PART-IV

Answer all questions.

7x4

4. ✓ Define integral domain and prove that a finite integral domain is a field. Is the converse true ?

OR

Let $a \in$ a ring R . Let $S = \{x \in R : ax = 0\}$. Show that S is a subring of R .

5. Let ϕ be a ring homomorphism from a ring to a ring to S . Then $\text{Ker } \phi = \{r \in R : \phi(r) = 0\}$ is an ideal of R .

OR

- ✓ Let R be a commutative ring with unity and A be an ideal of R . Then prove that R/A is a field iff A is maximal.

6. State and prove Division algorithm for $F[x]$.

OR

- ✓ Let $f(x) \in \mathbb{Z}[x]$. if $f(x)$ is reducible over \mathbb{Q} , then prove that it is reducible over \mathbb{Z} .

7. ✓ Prove that in a principal ideal domain, an element is an irreducible iff it is a prime.

OR

Let $P(x)$ is an irreducible polynomial over a field F . Prove that the ideal generated by $P(x)$ in $F(x)$ is a maximal ideal.



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2025

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*Answer **all** questions.*

PART-I

1. Answer all Questions.

1x12

- a. What is the derived set of set $A = \left\{ \frac{1}{n} : n \in \mathbb{N} \right\}$ in Euclidean Metric space ?
- b. Let X be a nonempty set and d on X defined by
$$d(x, y) = \begin{cases} 1, & x \neq y \\ 0, & x = y \end{cases}$$
 then d is called _____ metric.
- c. What can be said about Uniform continuity of the function $f : \mathbb{R}_U \rightarrow \mathbb{R}_U$ defined by $f(X) = X^2$?
- d. Any subspace of a second countable space is also second countable. (True/False)
- e. What can you say about the continuous image of a connected space ?
- f. Is $Y = \{x \in \mathbb{R} : 1 < x < 2\}$ dense in \mathbb{R} ? (Yes / No)

(Turn Over)

g. The distance between

$$a = \left\{ (x, y) \in \mathbb{R}^2, Y = \frac{1}{x} \neq 0 \right\} \text{ and}$$

$$b = \left\{ (x, y) \in \mathbb{R}^2, Y = 0 \right\} \text{ is } \underline{\hspace{2cm}}.$$

$$x, y \in \mathbb{R}^2$$

$$Y = \frac{1}{x} \neq 0$$

$$Y_y = d(y, z) : d$$

h. A composition of two uniformly continuous mapping is again Uniformly continuous. (True/False)

i. Let $A = \emptyset$ and $B = \mathbb{R}$ then $A^0 \cup B^0 = \underline{\hspace{2cm}}$.

j. The Singleton set $\{x\}$ on any metric space x is connected. (True/false)

k. A totally bounded metric space is also bounded. True or false.

l. In a metric space, any two disjoint sets are always separated. Write true or false.

PART-II

2. Answer any eight questions.

2x8

- Define Euclidean metric on \mathbb{R}^n .
- Let (X, d) be a metric space and $x \in X$, then define local base at X .
- Define a Cauchy sequence in a metric space.
- Define compact metric space.
- Is the subset $\{3n+1, n \in \mathbb{Z}\}$, $\{3n, n \in \mathbb{Z}\}$ and $\{3n+2, n \in \mathbb{Z}\}$ forms an open cover of \mathbb{Z} . Explain.
- Define the local base of an element X in a Metric Sapce (X, d) .
- Let (X, d) be a metric space and A, B be subsets of X . Show that $A \subseteq B \Rightarrow A^0 \subseteq B^0$.
- Define Isometric functions.

- i. Define Pseudo-Metric space.
 j. Let X be a complete space. Then does the mapping $T: X \rightarrow X$ have a fixed point? Justify.

PART-III

3. Answer any eight of the following questions. 3x8

- a. Prove that the Cauchy Sequence of real numbers is convergent.
 b. Prove that in any metric space (x, d) each open ball is an open set.
 c. If (X, dx) , (Y, dy) and (Z, dz) are metric spaces and if $f: X \rightarrow Y$ and $g: Y \rightarrow Z$ are continuous, then prove that $g \circ f: X \rightarrow Z$ is also continuous.
 d. Prove that in any metric space, there is a countable base at each point.
 e. Prove that two metrics d_1 and d_2 on a non-empty set X are equivalent if there exists a constant K such that

$$\frac{1}{k} d_2(x, y) \leq d_1(x, y) \leq k d_2(x, y), \forall x, y \in X.$$

- f. Show that $f: \mathbb{R} \rightarrow (-1, 1)$ defined by $f(x) = \frac{x}{1+|x|}$ is a homomorphism.
 g. Let (X, d) be a metric space and A, B be subsets of X . Then prove that $(A \cup B)^0 \supseteq A^0 \cup B^0$

- h. Let $f(x) = \sin\left(\frac{1}{x}\right), x \in \mathbb{R} - \{0\}$. Prove that the function f can't be extended to a continuous function on \mathbb{R} .

- i. If $X = Y_1 \cup Y_2$ and Y_1 is of category I while X is of category II, then prove that Y_2 must be category II.

(3)

(Turn Over)

- j. Let $f: [-1, 1] \rightarrow [-1, 1]$. show that there is a fixed point $C \in I$ such that $f(C) = C$.

PART-IV

Answer all questions.

7x4

4. Prove that the space l^p is complete.

OR

State and prove Cantor's theorem.

5. Let $T: X \rightarrow X$ be a contraction of the complete metric space (X, d) . then prove that T has a unique fixed point.

OR

- ✓ Let (X, d) be a metric space. Then prove that the following statements are equivalent.

- (X, d) is disconnected
 - There exist a continuous mapping of (X, d) onto the discrete two element space (X_0, d_0)
6. Prove that $f: X \rightarrow Y$ is continuous on X iff $f^{-1}(G)$ is open in X for all open subsets G and Y .

OR

- ✓ Show that the sequence $\{f_n\}_{n \geq 1}$ defined by

$f_n(x) = \tan^{-1}(nx), x \geq 0$ is uniformly convergent on $[\alpha, \infty)$ when $\alpha > 0$, but not uniformly convergent on $[0, \infty)$.

7. If f and g are two continuous maps on a metric space (X, d) then using $\epsilon - \delta$ method prove that $f+g$ and fg are continuous on X .

OR

- ✓ Prove that in a metric space, every convergent sequence has a Unique limit.



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